

Incorporating local surrogates into large-scale deterministic optimisation models for integrated decision-making in complex systems

Michael Short

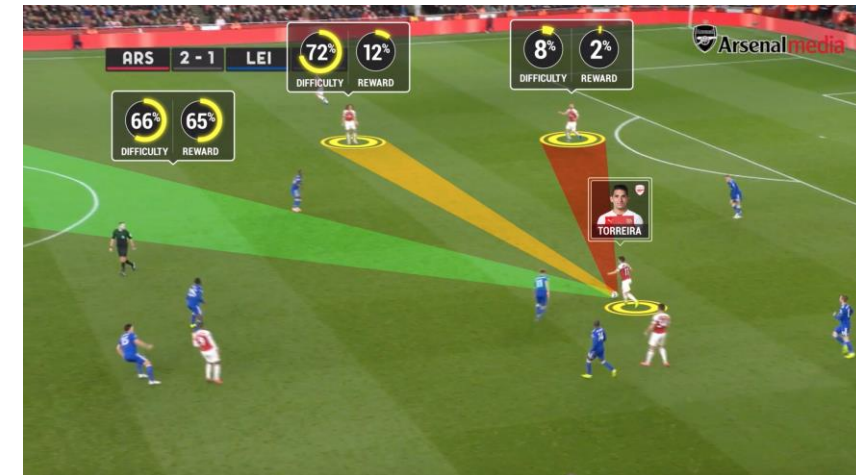
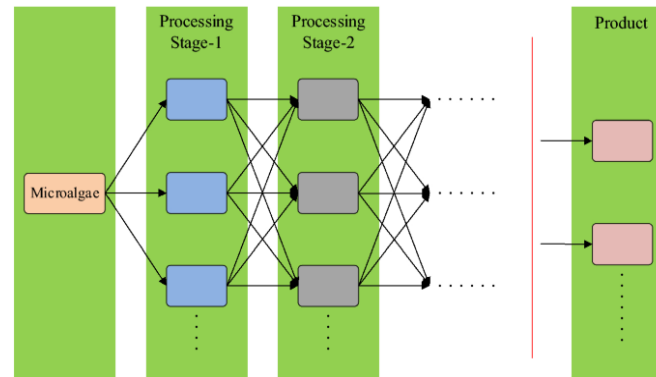
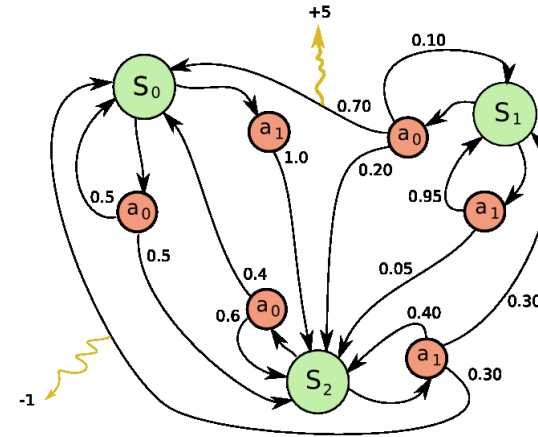
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Modern decision-making and need for integrated platforms

- Strategic, tactical, and operational
- Real-time optimisation
- Considering uncertainty
- Multi-objective
- Large-scale (degrees of freedom)
- Data and machine learning



Short research group @ Surrey

Combining data-driven and first-principles models to develop multi-scale models and software, from molecules to supply chains, to deliver optimal solutions to decision-makers.

Challenges and Opportunities:

Multi-scale and tractability

Ease of use and mathematical complexity

Data-driven and non-mechanistic modelling

Incorporating uncertainty and non-technical aspects

Applications for integrated decision-making and Sustainability

Group research areas:

Sustainable energy systems and bioenergy

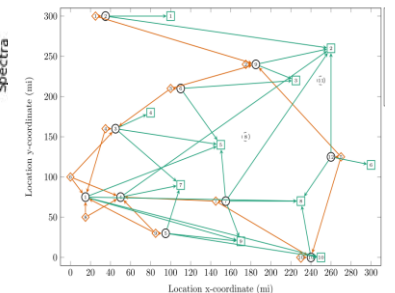
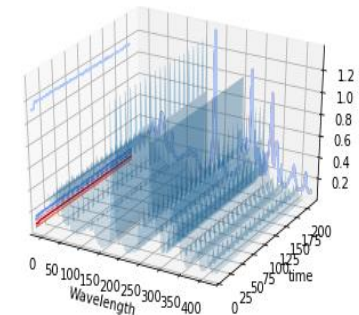
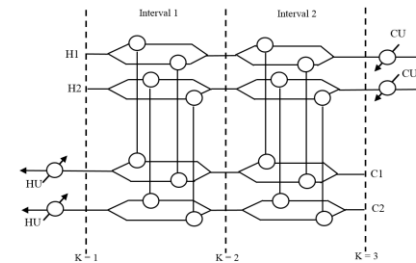
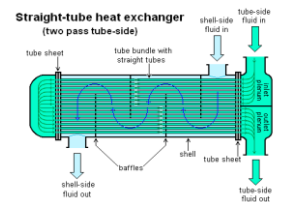
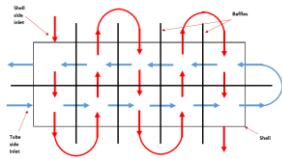
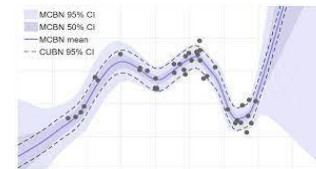
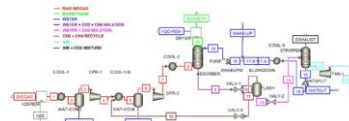
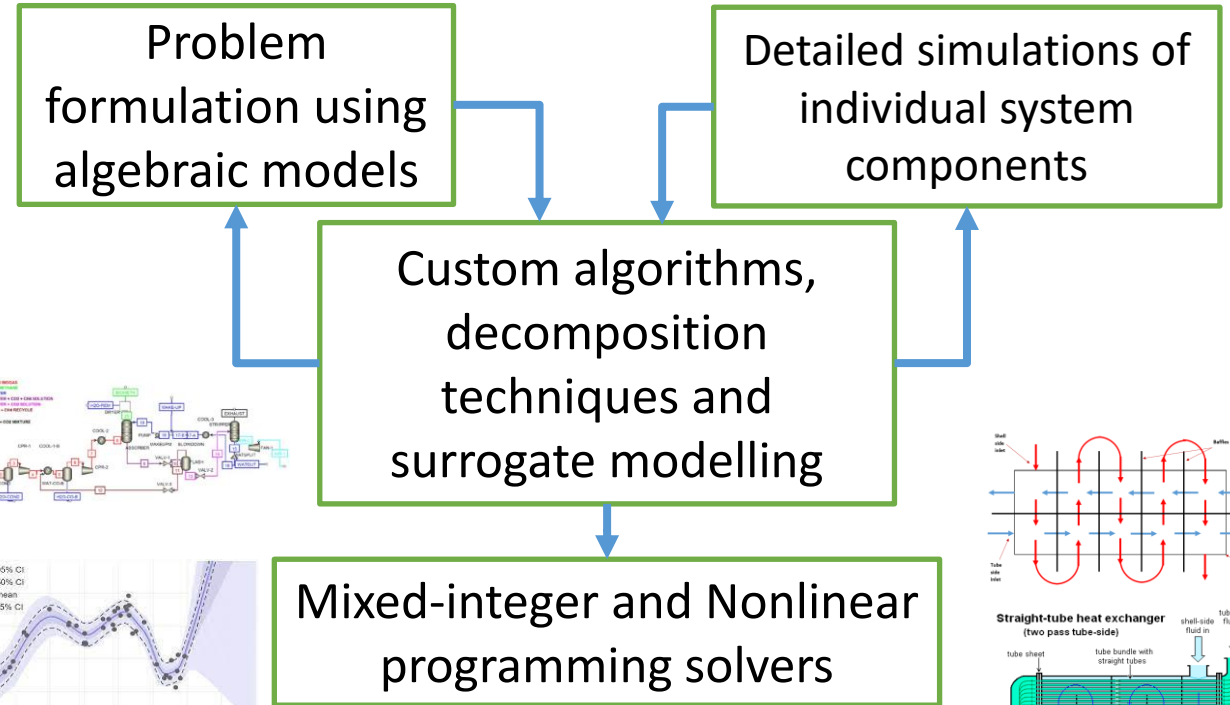
Model predictive control and real-time optimisation

Parameter estimation

Flowsheet optimisation

Non-convex multi-scale optimisation

Specialised Decision-support Software



Solving large-scale (mixed-integer) nonlinear problems

Applications to:

- Design of heat-integrated chemical processes
- Building energy control
- Biogas optimisation and control

Heat-Integrated Process Synthesis

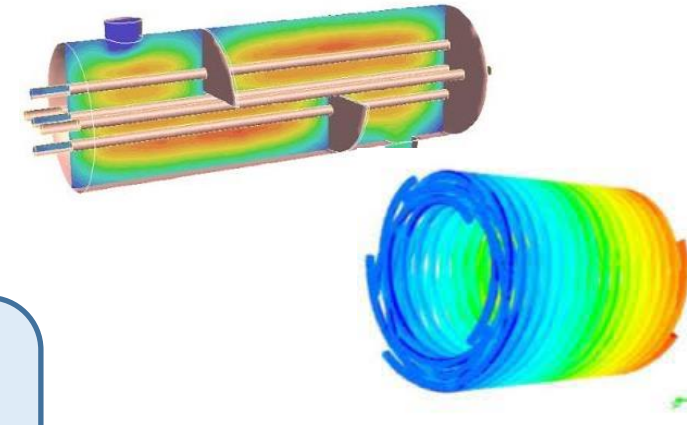
Network Scale



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- Optimisation model
- Modeled using primary design equations
- Less accurate and maybe practically infeasible

Equipment Scale



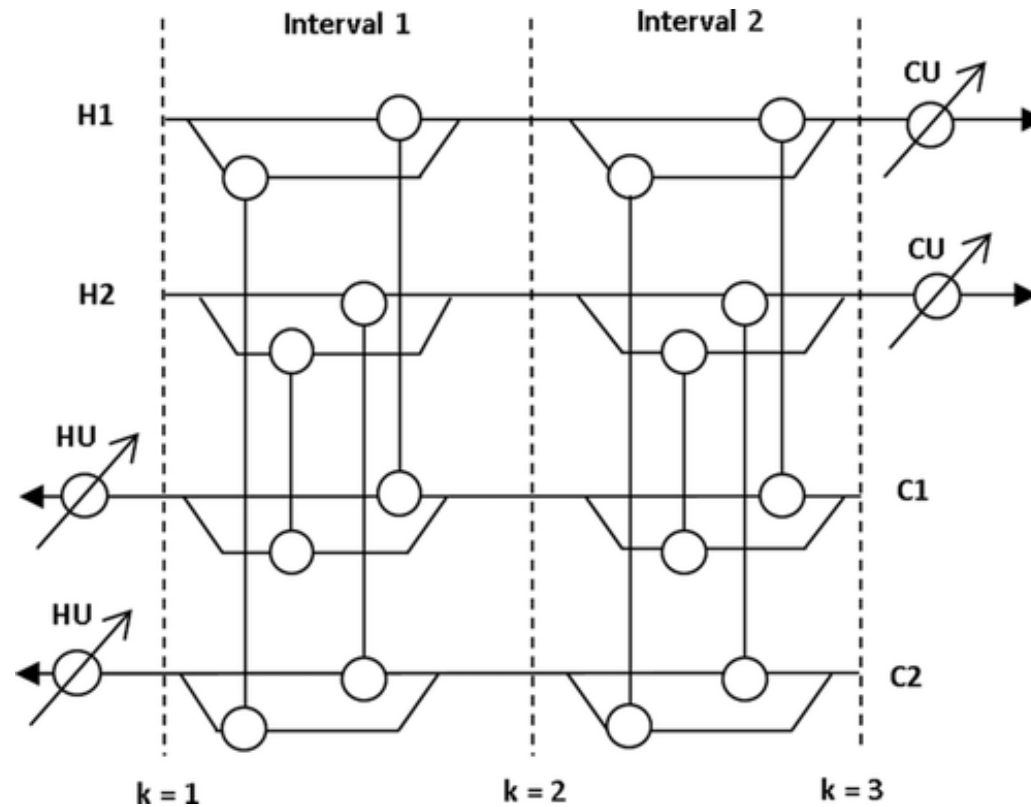
- First-principles based design model (DAE)
- Computationally tractable method (Trust-Region)

- Simulation based model
- Modeled using PDE conservation laws
- High accuracy but becomes intractable

DAE - Differential Algebraic Equations
PDE - Partial Differential Equations

HENS superstructures

Can use this for
mass exchange
as well

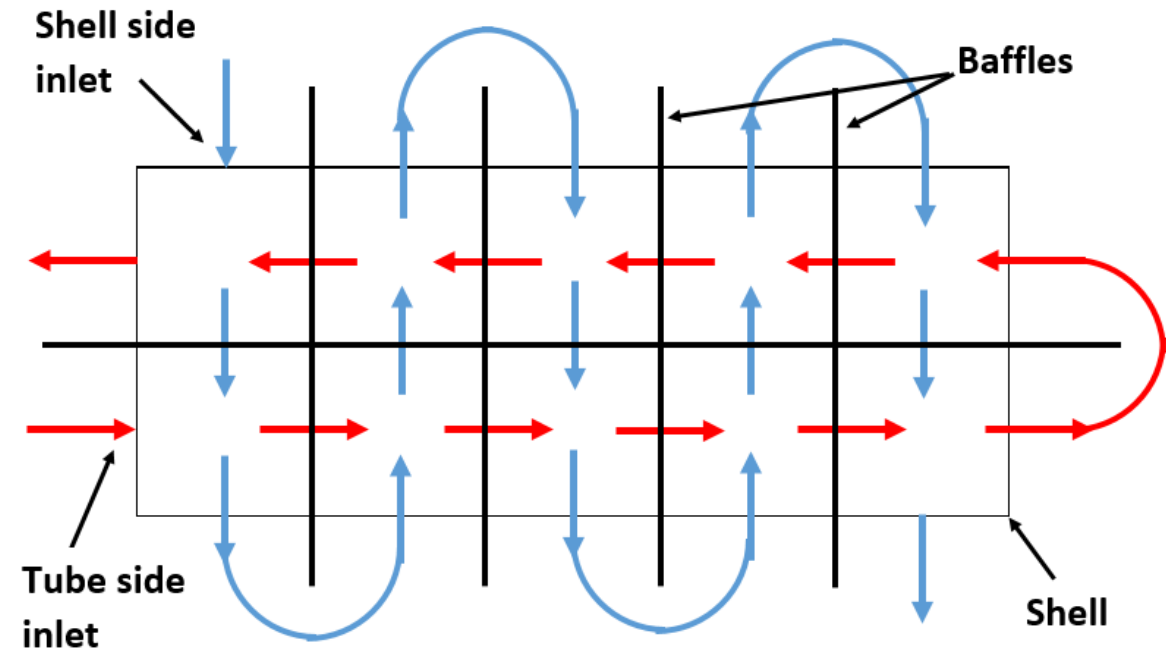
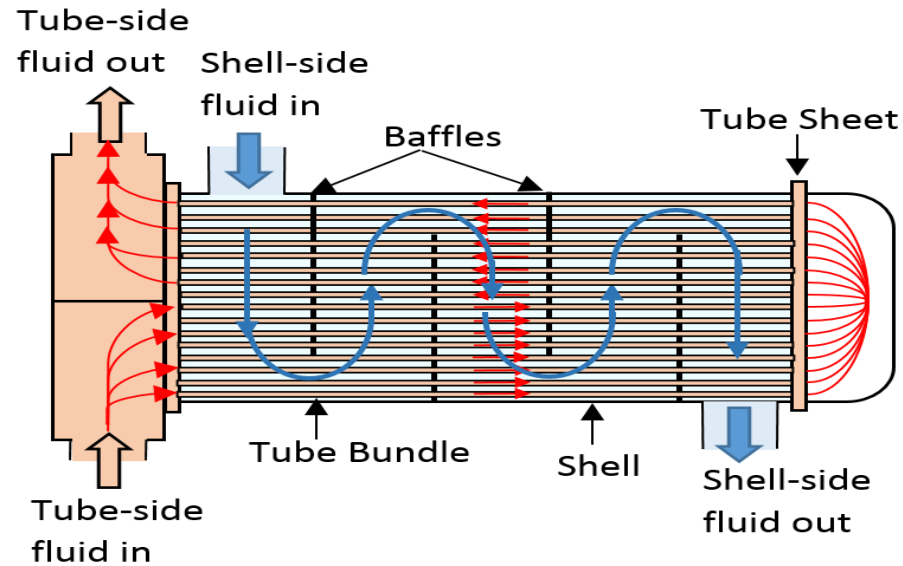


Yee and Grossmann, 1990, Simultaneous optimization models for heat integration—II. Heat exchanger network synthesis, Computers and Chemical Engineering, 14(10), 1165-1184

$$\begin{aligned}
\min \quad & \left[\sum_{i \in H} CUC qc_i + \sum_{j \in C} HUC qh_j + CF \left(\sum_{i \in H} \sum_{j \in C} \sum_{k \in K} z_{ij,k} \boxed{\phantom{q_{i,j,k}}} + \sum_{i \in H} zcu_i + \sum_{j \in C} zhu_j \right) \right. \\
& + \sum_{i \in H} \sum_{j \in C} \sum_{k \in K} \boxed{\phantom{q_{i,j,k}}} AC \left(\boxed{\phantom{q_{i,j,k}}} \frac{q_{i,j,k}}{(U_{i,j,k})(LMTD_{i,j,k})} \right)^{AE} \\
& \left. + \sum_{i \in H} AC \left(\frac{qc_i}{(U_i)(LMTD_i)} \right)^{AE} + \sum_{j \in C} AC \left(\frac{qh_j}{(U_j)(LMTD_j)} \right)^{AE} + \right. \\
& \left. \boxed{\phantom{q_{i,j,k}}} \right]
\end{aligned}$$

- s.t. Heat balances, temperature constraints, big-M constraints, bounds
- LMTD approximations are commonly used

Heat Exchanger Design Model

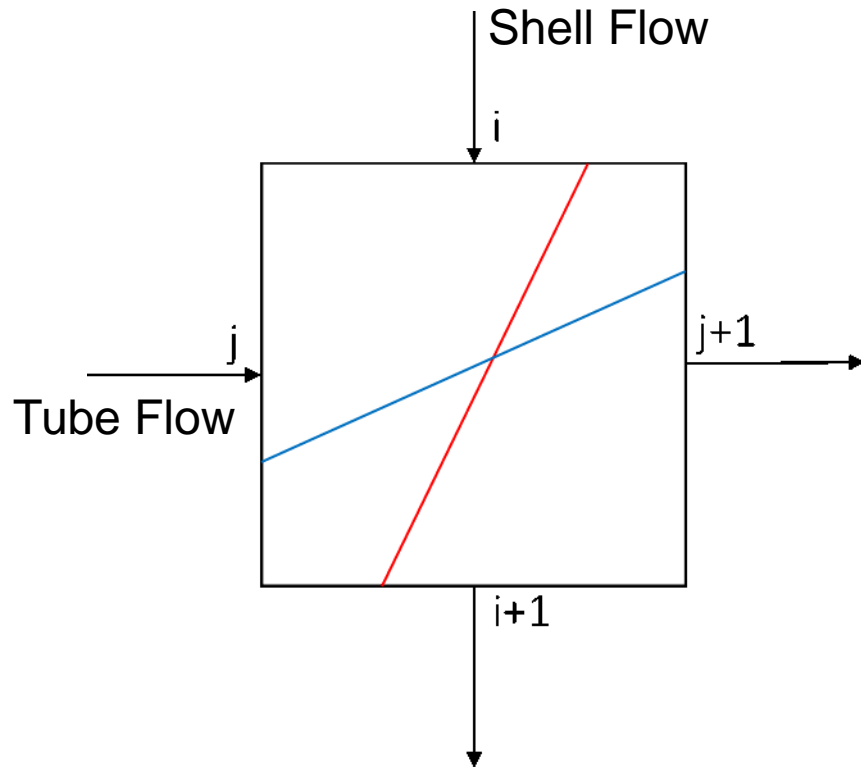


- Represent the shell and tube heat exchanger as a cascade of small elements
- Formulate the mass and energy conservation equations inside each element
- Correlate the exchanger area inside element with design variables like number of tubes etc.

DAE Model

<https://doi.org/10.1002/aic.17056>

Discrete Element



Discrete Algebraic Form

- 2D Heat Equation

$$\rho C_p \left(u_x \frac{\partial T}{\partial x} + u_y \frac{\partial T}{\partial y} \right) = k \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right) + q_v$$

- Can be simplified

$$C_h \frac{dT}{dA} + U(T - t) = 0$$

$$C_c \frac{dt}{dA} - U(T - t) = 0$$

C - Heat Capacity, A - Heat Exchanger Area

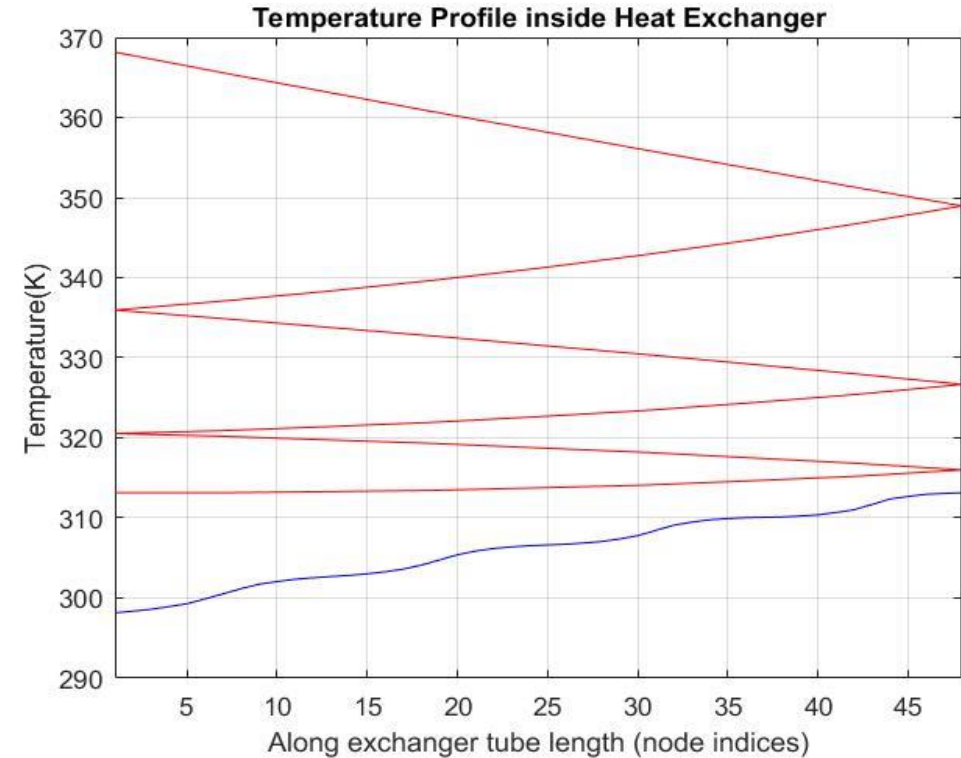
U - Overall Heat Transfer Coefficient

$$C_h \left(\frac{T_{i+1} - T_i}{2} \right) + U\Delta A \left(\frac{T_{i+1} - t_{j+1}}{3} \right) + U\Delta A \left(\frac{T_i - t_j}{6} \right) = 0$$

$$C_c \left(\frac{t_{j+1} - t_j}{2} \right) - U\Delta A \left(\frac{T_{i+1} - t_{j+1}}{3} \right) - U\Delta A \left(\frac{T_i - t_j}{6} \right) = 0$$

Example

	Mizutani et al. (2003)	Onishi et al. (2013)	LMTD Solution	Discrete Model (fixed L_t)	Discrete Model (variable L_t)
Total Cost(\$/yr)	5250.00	5134.21	5157.25	5279.28	5169.21
Area Cost(\$/yr)	2826.00	3175.61	3045.50	3041.44	3077.48
Pumping Cost(\$/yr)	2424.00	1958.59	2111.75	2237.84	2091.73
Area(m^2)	202	247.22	230.3	229.8	234.4
Duty(kW)	4339	4339	4339	4339	4339
LMTD(K)	30.78	31.27	30.78	N/A	N/A
F_t	0.812	0.823	0.823	N/A	N/A
N_{tp}	2	2	8	8	8
$D_s(m)$	0.69	0.79	1.15	1.15	1.18
N_t	832	616	790	790	842
N_b	8	17	4	4	4
$d_o(mm)$	15.9	19.05	25.4	25.4	25.4
$d_i(mm)$	12.6	16.60	21.18	21.18	21.18
$p_t(mm)$	19.88	25.4	31.75	31.75	31.75
$L_t(m)$	4.88	6.706	3.658	3.658	3.49
$v_t(m/s)$	-	1.04	1.03	1.07	1.00
$v_s(m/s)$	-	0.50	0.41	0.41	0.42
$h_t(W/m^2.K)$	6480	4356.7	1951.1	2022.9	1919.3
$h_s(W/m^2.K)$	1829	1880.2	2728.4	2729.8	2761.3
$U(W/m^2.K)$	860	682.2	724.2	725.2	710.8
$\Delta P_t(kPa)$	22.68	15.92	26.85	29.43	25.26
$\Delta P_s(kPa)$	7.49	10.61	8.92	8.93	9.55
Hot fluid allocation	Shell	Shell	Tube	Tube	Tube



Stream	$T_{in}(K)$	$T_{out}(K)$	$\dot{m}(kg/s)$	$\mu(Pa.s)$	$\rho(kg/m^3)$	$C_p(kJ/kg.K)$	$k(W/m.K)$
1	368.15	313.75	27.78	3.4e-04	750	2.840	0.19
2	298.15	313.15	68.88	8.0e-04	995	4.200	0.59

$a_{cost}=123, b_{cost}=0.59, c_{cost}=1310$

NLP model for packed columns

Mass transfer equations:

$$\frac{dM}{dz} = N_{total}$$

Pratt's correlation for mass transfer coefficient

$$ky_{r,l,k} = \frac{G'_{r,l,k}}{\epsilon_{r,l,k}} \cdot a_G \cdot \left(\frac{de_{r,l,k} \cdot G'_{r,l,k}}{\epsilon_{r,l,k} \cdot \mu_{r,l,k}} \right)^{-0.25} \cdot Sc^{-0.667} \omega e^{\beta Lp}$$

Henry's coefficient is a function of temperature

$$L_{r,l,k} \frac{dx_{r,l,k}}{dz} = Flux_{r,l,k,tt}$$

$$G_{r,l,k} \frac{dy_{r,l,k}}{dz} = Flux_{r,l,k,tt}$$

$$Flux_{r,l,k,ii,jj} = ky_{r,l,k} \cdot ai_{r,l,k} \cdot A_{r,l,k} \cdot (Cr_{r,l,k,ii,jj} - He \cdot Cl_{r,l,k,ii,jj})$$

Flooding equations:

$$FloodPoint_{r,l,k} = \frac{249.089}{0.3048} * 0.12 * (0.3048 * PackFact_{r,l,k})^{0.7}$$

$$Pdrop_{r,l,k} = (94 \cdot \left(\frac{ReL_{r,l,k}^{1.11}}{ReG_{r,l,k}^{1.8}} + 4.4 \right) \cdot 6 \cdot \left(1 - \frac{\epsilon_{r,l,k}}{de_{r,l,k} * \epsilon_{r,l,k}^3} \right) \cdot \rho_r \cdot G'_{r,l,k}^2)$$

$$G_{r,l,k} = A_{r,l,k} \cdot G'_{r,l,k}$$

$$ReL_{r,l,k} = \frac{\rho_l \cdot L'_{r,l,k}}{\mu_l \cdot ai_{r,l,k}}$$

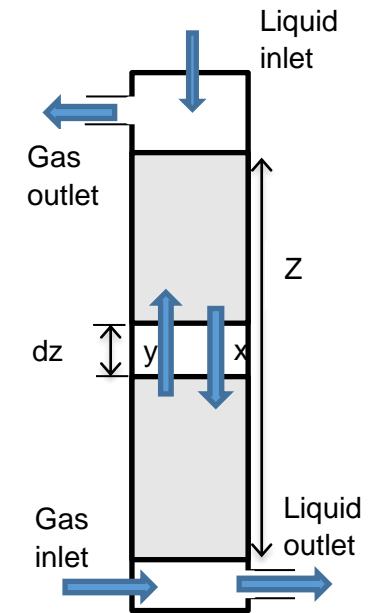
$$FloodPoint_{r,l,k} \geq Pdrop_{r,l,k}$$

$$L_{r,l,k} = A_{r,l,k} \cdot L'_{r,l,k}$$

$$ReR_{r,l,k} = \frac{\rho_r \cdot G'_{r,l,k}}{\mu_r \cdot ai_{r,l,k}}$$

$$A_{r,l,k} = \frac{\pi}{4} \cdot (D_{r,l,k})^2$$

Solved for every exchanger selected by MINLP simultaneously



Trust Region Filter Optimisation

- TRF is useful for rigorous optimisation with reduced/surrogate model
- High-fidelity ‘truth’ exchanger models may be too expensive
- Deriving reduced models (RMs):
 - Solutions must match truth model
 - Must recognise the same optimum (same KKT conditions satisfied)
 - Must be stable – objectives remain bounded and sufficient improvement
- Idea is to have an optimisation problem with certain parts as “black box” and certain as “glass box” models

$$\begin{aligned} \min_{z,w} \quad & f(z, w, t(w)) \\ \text{s.t.} \quad & h(z, w, t(w)) = 0 \\ & g(z, w, t(w)) \leq 0 \end{aligned}$$

Trust Region Filter Optimisation

$$\begin{aligned}
 \min_x \quad & f(x) \\
 \text{s.t.} \quad & h(x) = 0 \\
 & y = r_k(w) \\
 & g(x) \leq 0 \\
 & \|x - x_k\| \leq \bar{\Delta}_k
 \end{aligned}
 \quad x^T = [z^T, w^T, y^T]$$

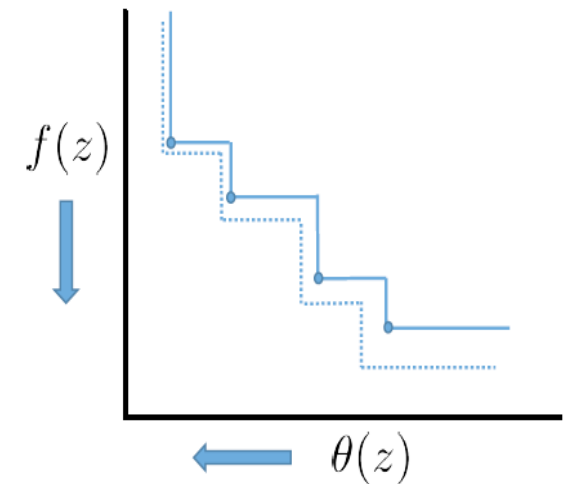
(TRSP)

$$s_k := x_{s,k}^* - x_k \quad \text{step}$$

$$\theta(x_k) = \|y_k - t(w_k)\| \quad \text{infeasibility}$$

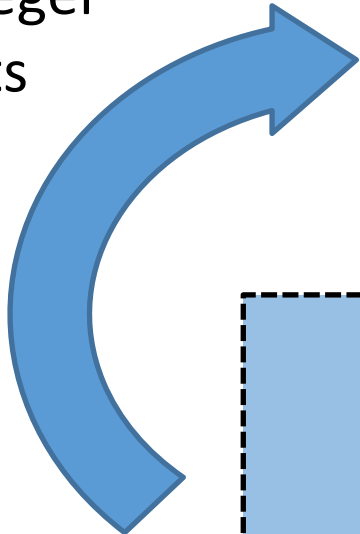
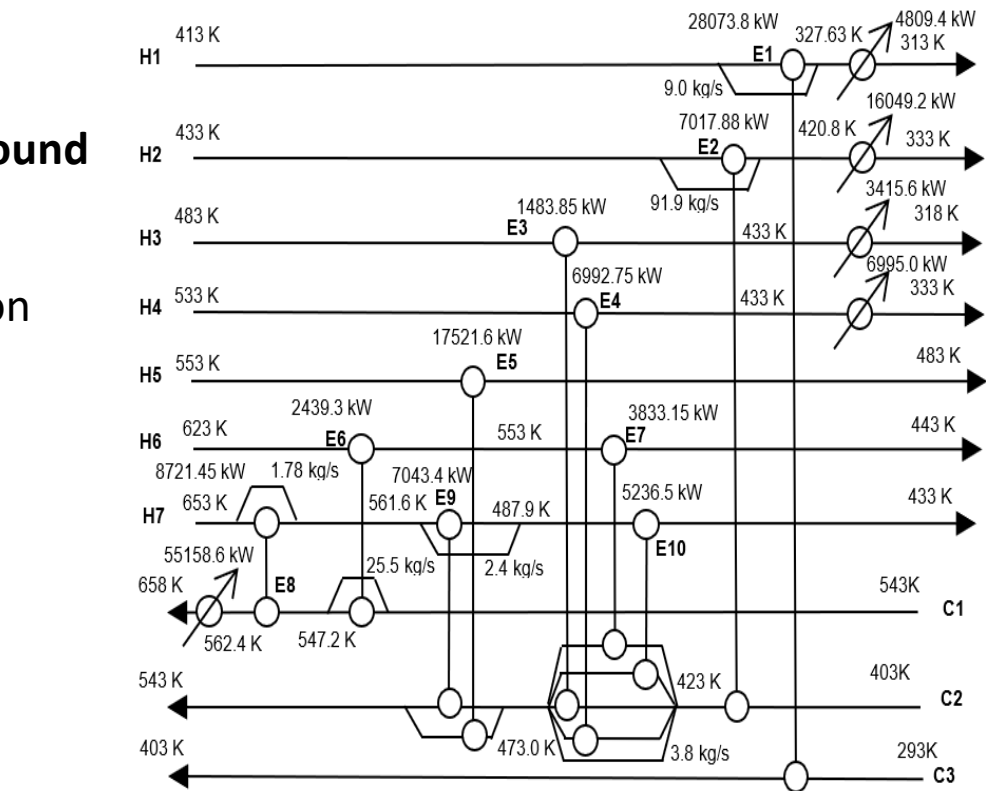
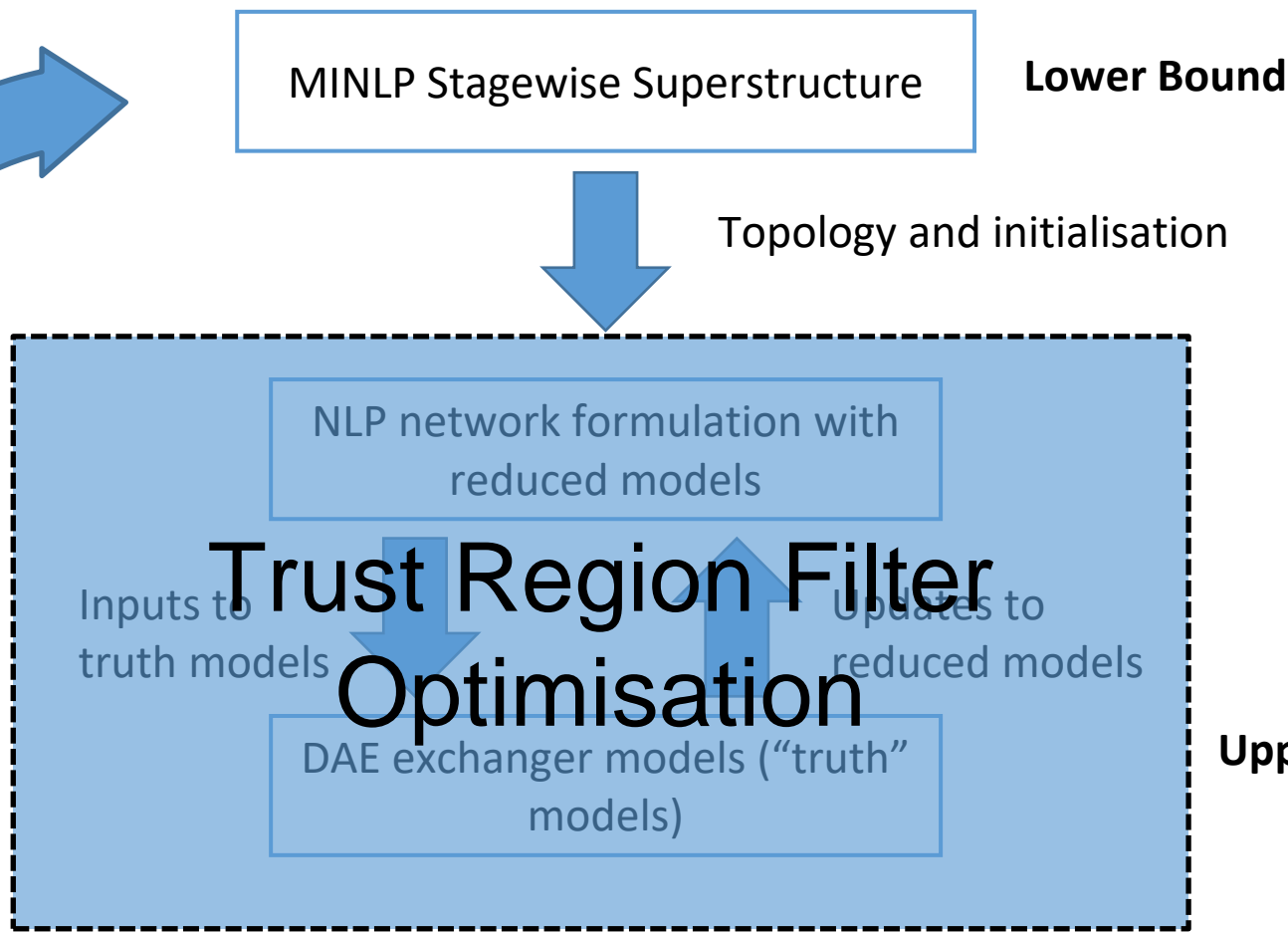
$$r_k(w) = \tilde{r}(w) + (t(w_k) - \tilde{r}(w_k)) + (\nabla t(w_k) - \nabla \tilde{r}(w_k))^T (w - w_k)$$

$\hat{r}(w)$ can be any model (shortcut-based, sampling based or constant)



Process synthesis framework

Integer Cuts

Upper Bound



Computers & Chemical Engineering
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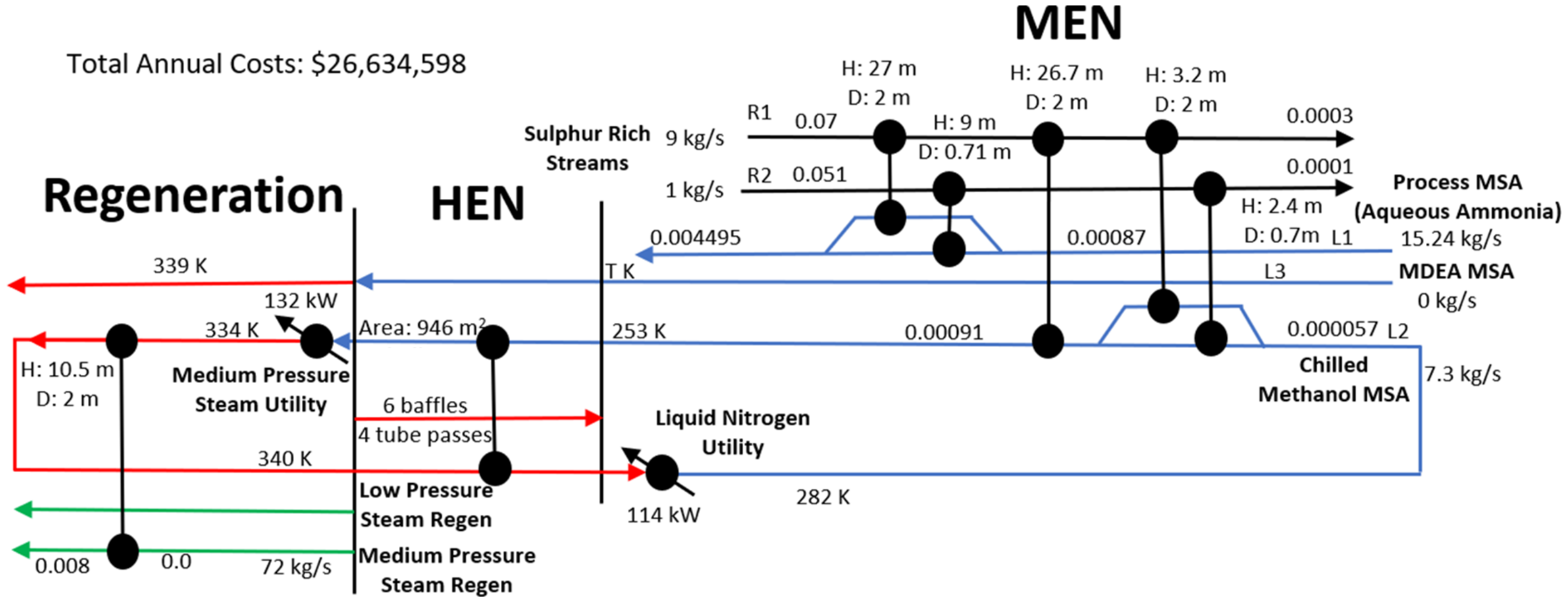


A trust region framework for heat exchanger network synthesis with detailed individual heat exchanger designs

Soif R. Kozi^a, Michael Short^b, Lorenz T. Biegler^a

CHAMENS results

Total Annual Costs: \$26,634,598



Optimal model-based decision-making software for complex nonlinear systems



KIPET – Kinetic Parameter Estimation Toolkit

In collaboration with Carnegie Mellon University, Syngenta, Dow, and Eli Lilly and Company

Open-source software for fast kinetic parameter estimation and chemometrics from spectroscopic data and other sources using nonlinear programming for real-time monitoring and control

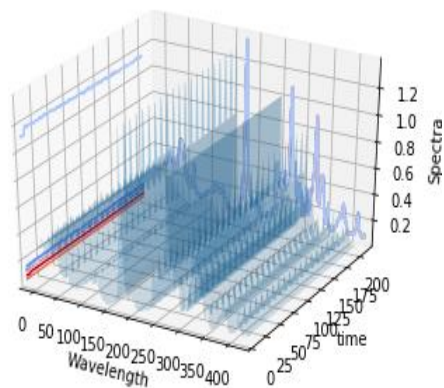
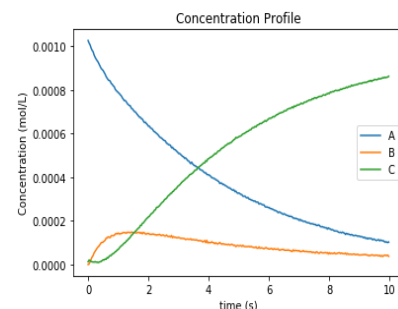
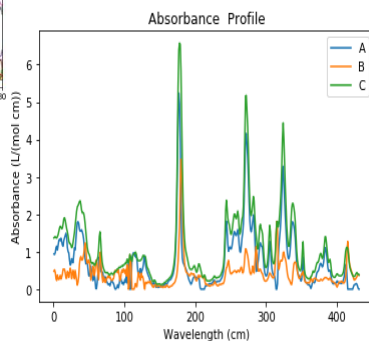
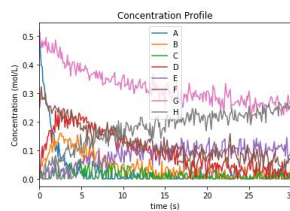
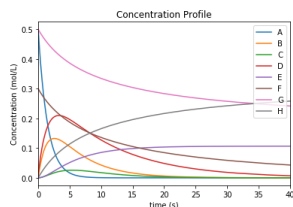


$$\min \sum_{i=1}^{np} \sum_{l=1}^{nlp} \left(d_{i,l} - \sum_{k=1}^{nc} c_k(t_i) s_k(\lambda_l) \right)^2 / \delta^2 + \sum_{i=1}^{np} \sum_{k=1}^{nc} (c_k(t_i) - z_k(t_i))^2 / \sigma_k^2$$

$$\text{s.t. } \sum_{m=0}^K \dot{l}_m(\tau) z_{jm} - h_j \cdot f(z_{jm}, \theta) = 0, j = 1..ne, m = 1..K$$

$$z^k(t_i) = \sum_{m=0}^K l_m(\tau) z_{jm}, \tau = (t_i - tp_{j-1}) / (tp_j - tp_{j-1})$$

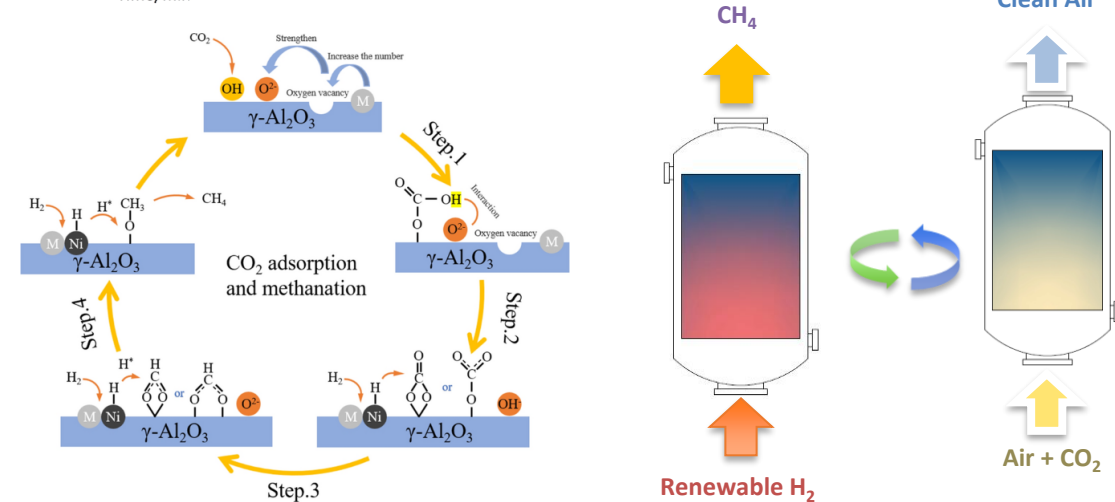
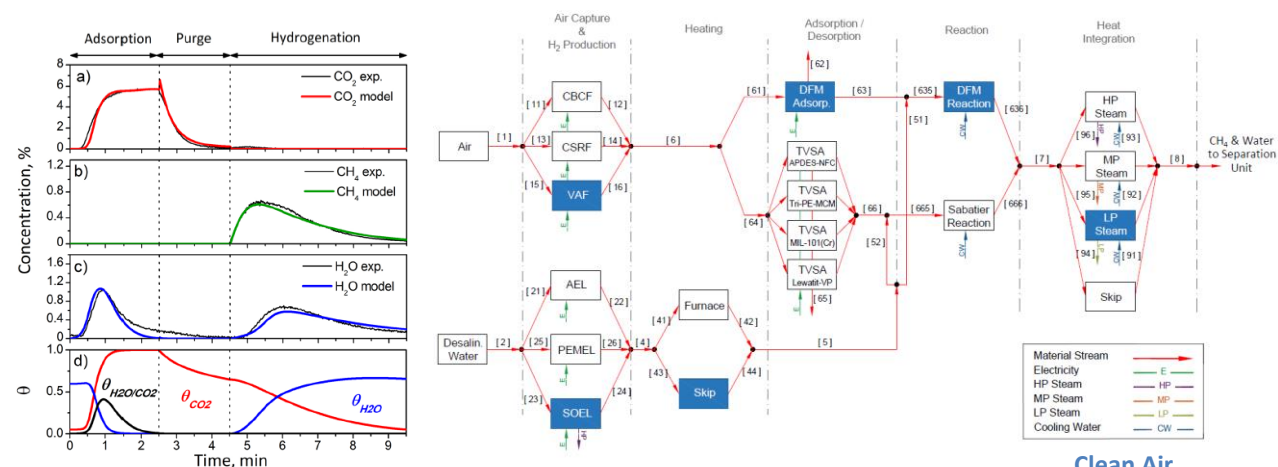
$$C \geq 0, S \geq 0$$



Techno-Economic Analysis of Dual Function Material for DAC

Using kinetic modelling and superstructure approaches to assess DFMs as a potential DAC

Funding from the EPSRC
Adventurous Energy programme



ADVENT-AI: OPTIMISATION OF
BUILDING HEATING AND
VENTILATION USING
ARTIFICIAL INTELLIGENCE



$$\mathcal{M}(\Pi_{-N|k-1}, \hat{x}_{-N|k-1}, y(k), \dots, y(k-N)) :$$

$$\min_{x_{-N}, w_k} \Phi_{-N}(x_{-N|k}, \hat{x}_{-N|k-1}, \Pi_{-N|k-1}) + \dots$$

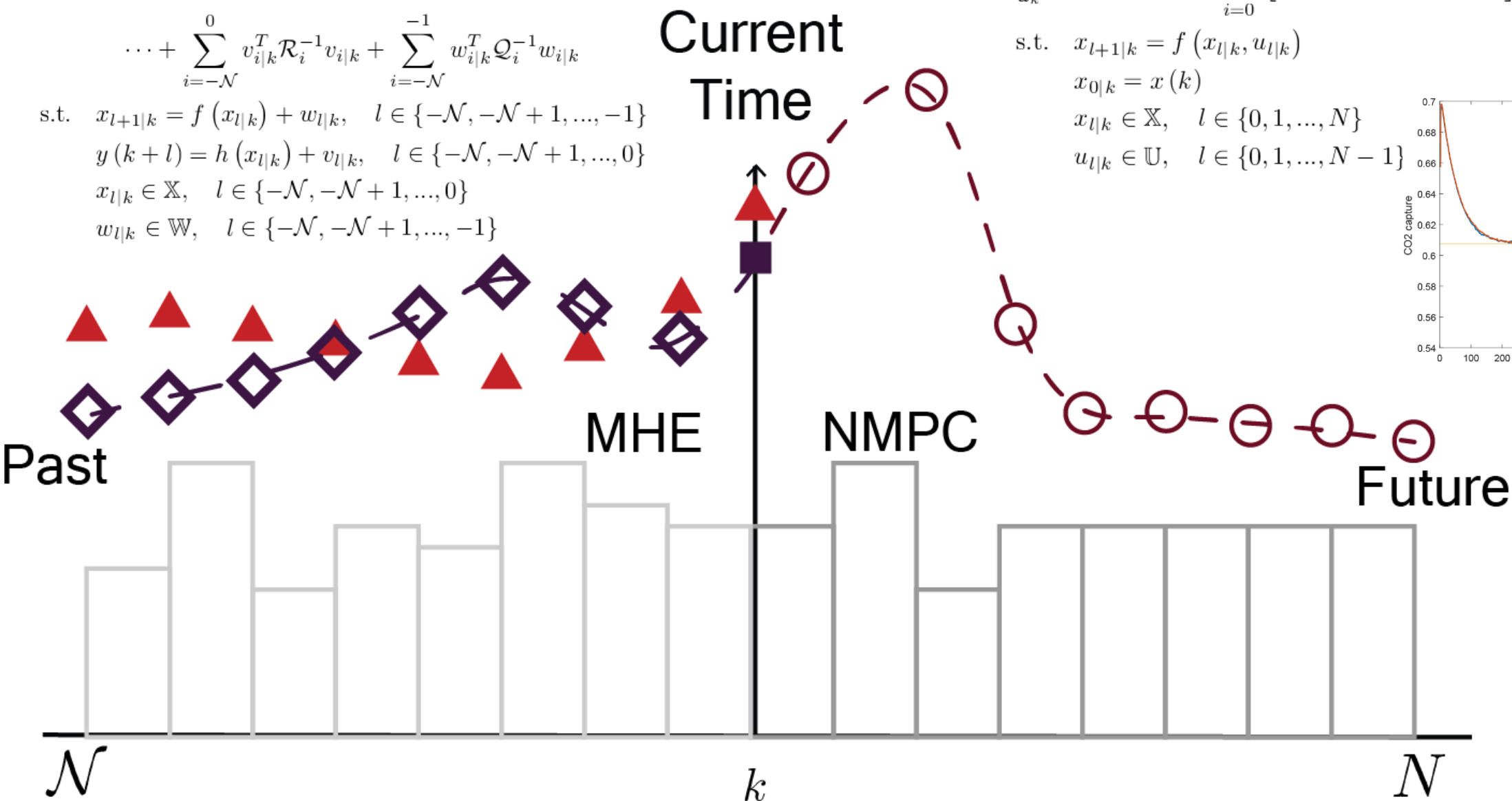
$$\dots + \sum_{i=-N}^0 v_{i|k}^T \mathcal{R}_i^{-1} v_{i|k} + \sum_{i=-N}^{-1} w_{i|k}^T \mathcal{Q}_i^{-1} w_{i|k}$$

$$\text{s.t. } x_{l+1|k} = f(x_{l|k}) + w_{l|k}, \quad l \in \{-N, -N+1, \dots, -1\}$$

$$y(k+l) = h(x_{l|k}) + v_{l|k}, \quad l \in \{-N, -N+1, \dots, 0\}$$

$$x_{l|k} \in \mathbb{X}, \quad l \in \{-N, -N+1, \dots, 0\}$$

$$w_{l|k} \in \mathbb{W}, \quad l \in \{-N, -N+1, \dots, -1\}$$



$$\mathcal{P}(x(k)) :$$

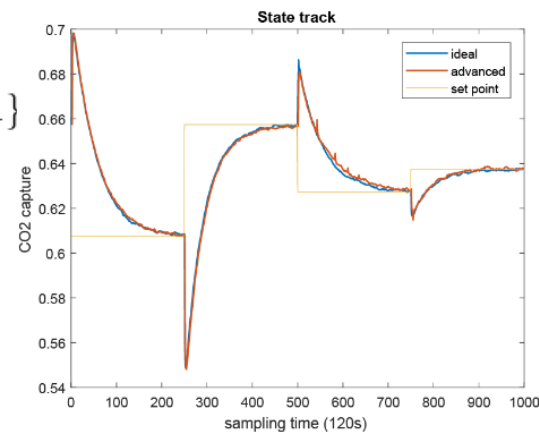
$$\min_{u_k} \varphi_N(x_{N|k}) + \sum_{i=0}^{N-1} [x_{i|k}^T Q x_{i|k} + u_{i|k}^T R u_{i|k}]$$

$$\text{s.t. } x_{l+1|k} = f(x_{l|k}, u_{l|k})$$

$$x_{0|k} = x(k)$$

$$x_{l|k} \in \mathbb{X}, \quad l \in \{0, 1, \dots, N\}$$

$$u_{l|k} \in \mathbb{U}, \quad l \in \{0, 1, \dots, N-1\}$$



ADVENT-AI - HOW IT WORKS



Immediate savings

Once installed, the solution immediately begins resulting in savings through smart energy management via a smart thermostat (based on current thermal comfort and occupancy)

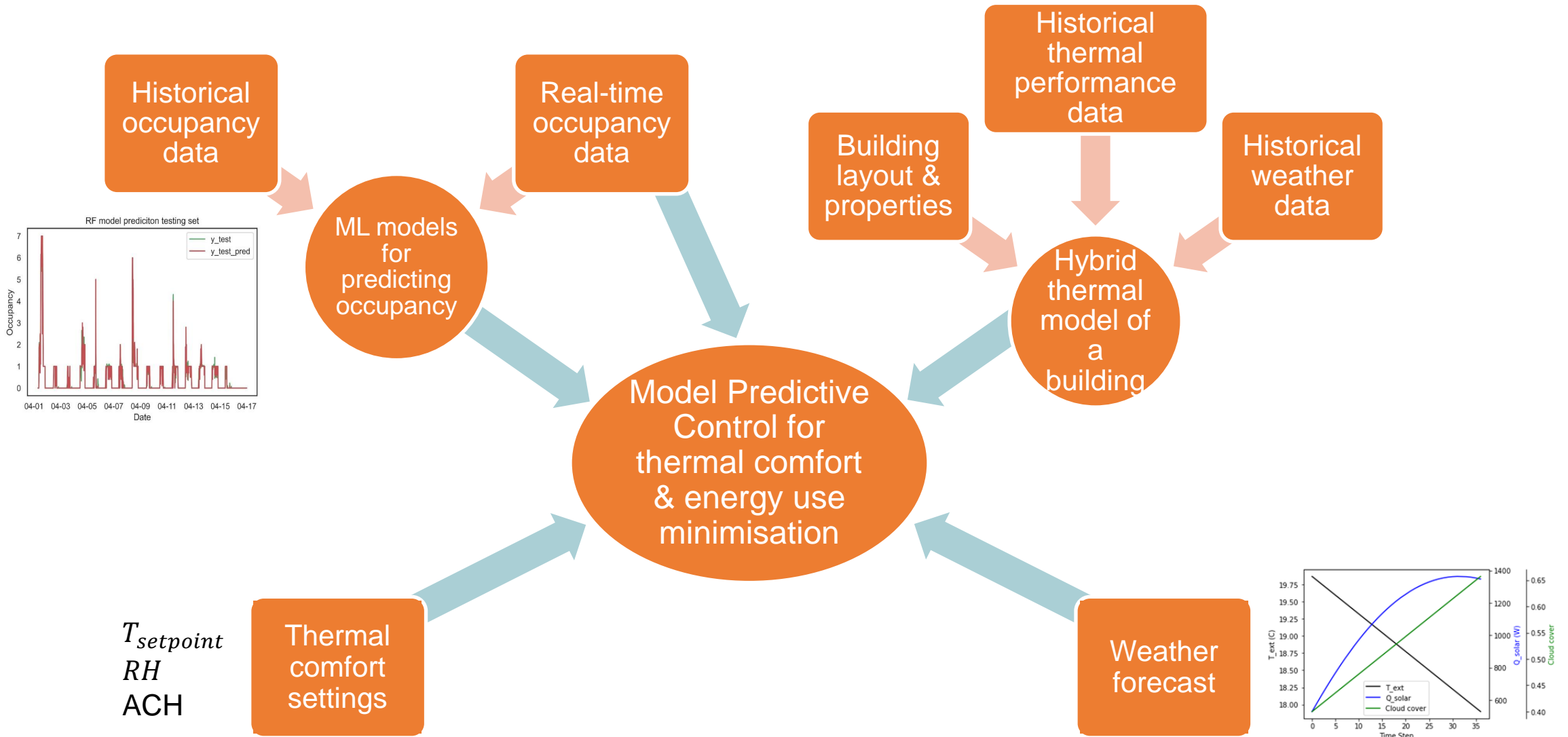
Model improvement

Over time, the model learns the thermal properties of the space as well as the occupancy patterns (e.g., in just 2 weeks, model can predict occupancy with 80% accuracy in initial studies)

Increasing returns

A combination of artificial intelligence and first-principles models is used to increase performance over time, taking advantage of dynamics within the space to save energy, reduce bills, and lower carbon emissions, while maintaining thermal comfort

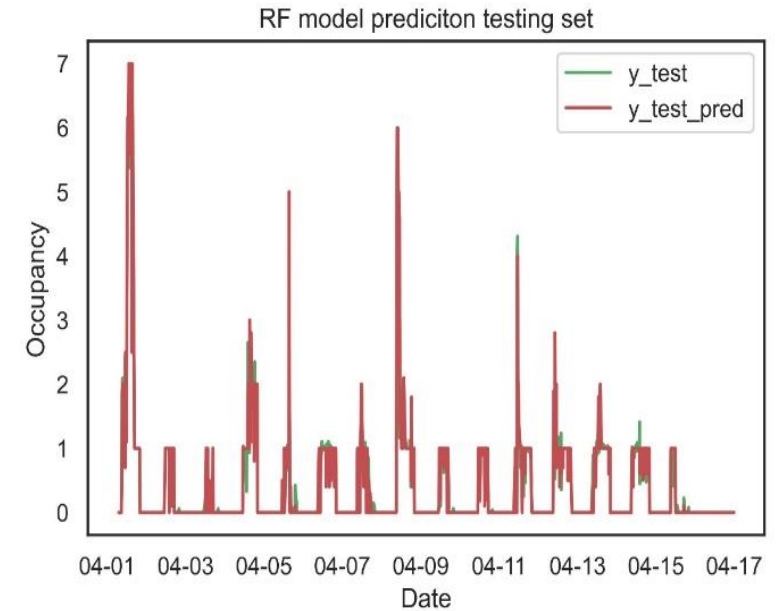
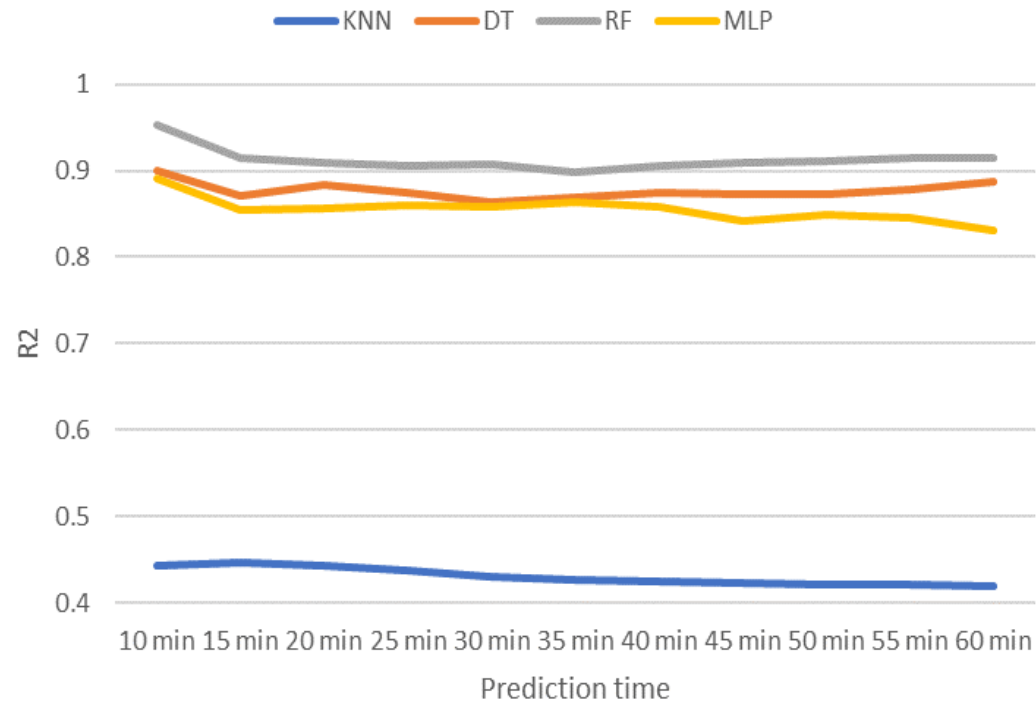
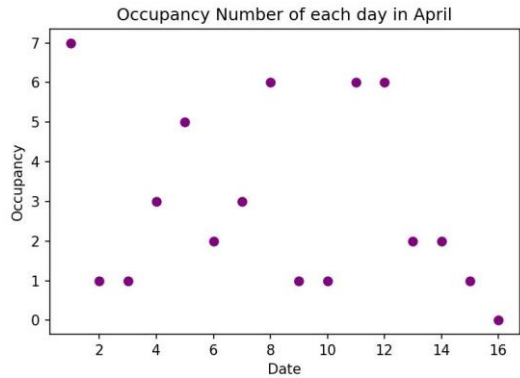
SMART MODEL PREDICTIVE CONTROL SYSTEM



OCCUPANCY MODEL



A rigorous assessment of different machine learning models was used to determine the occupancy prediction model based on data from DIREK Ltd.



R² for the occupancy prediction models with different number of outputs in 5 min frequency.



$$\int_{t_0}^{t_0+PH} \left[\alpha \frac{\dot{Q}_{heater}(t)}{Q_{heater}^{max}} + (1 - \alpha) H(N_{occupants}(t) - 0.5) \frac{(T(t) - T_{setpoint})^2}{\Delta T^2} \right] dt \rightarrow \min_{\dot{Q}_{heater}(t)}$$

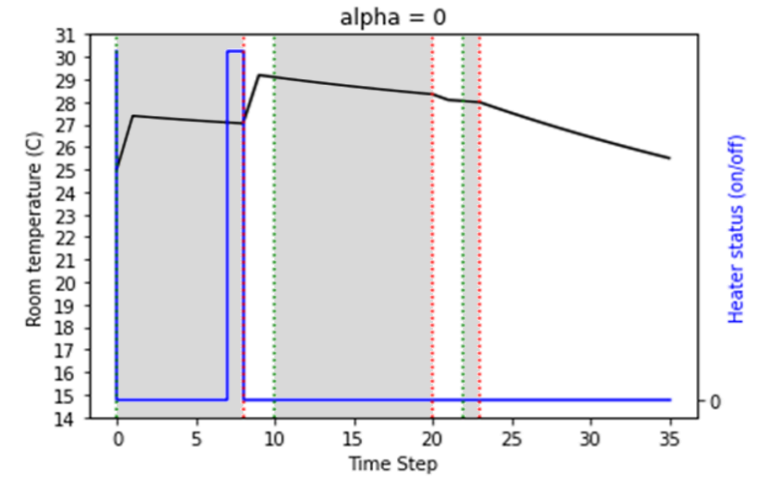
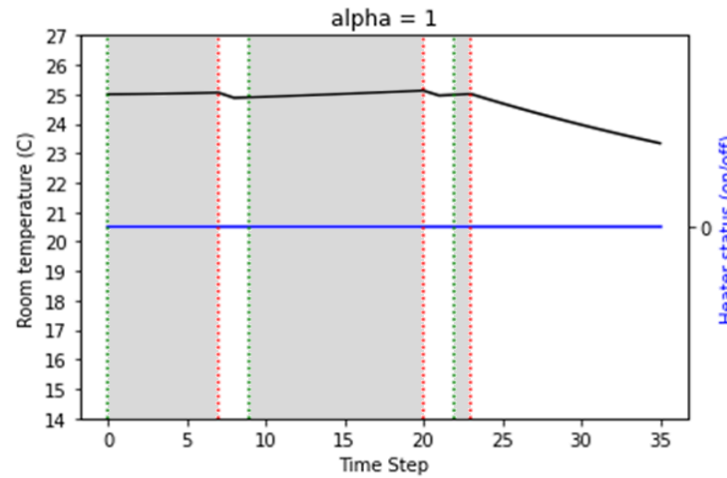
$$s. t. \quad T(t) \geq T_{setback}(t), \quad \forall t$$

$$0 \leq \dot{Q}_{heater}(t) \leq \dot{Q}_{heater}^{max}$$

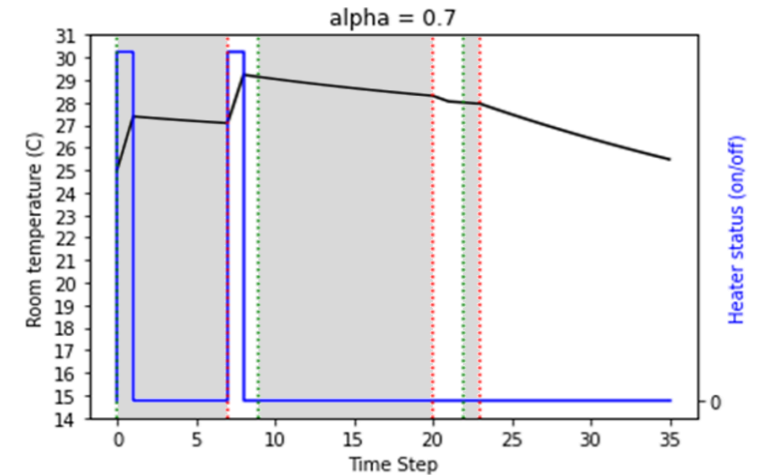
$$\frac{dQ}{dt} = \dot{Q}_{heater}(t) + \dot{Q}_{solar}(t) - \dot{Q}_{diffusion}(t, T, T_{ext}) - \dot{Q}_{convection}(t, T, T_{ext}) + \dot{Q}_{occupants}(t) + \dot{Q}_{equipment}(t)$$

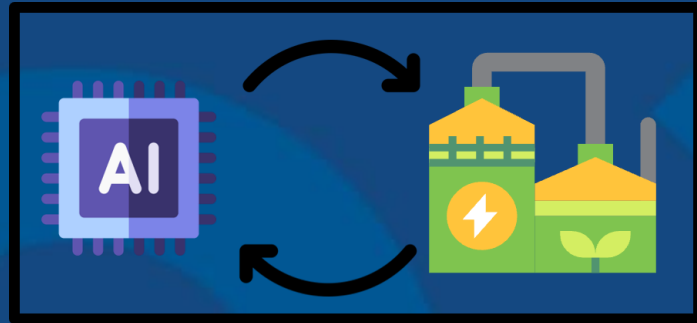
$$T(t_0) = T_{measured}(t_0)$$

CASE STUDY: A MEETING ROOM



- Temperature set point is 28°C with a tolerance of $\pm 1^\circ\text{C}$
- Thermal comfort is ensured when the space is predicted to be occupied (greyed intervals)
- Parameter α sets relative priorities of thermal comfort and energy saving:
 - $\alpha = 0$: thermal comfort only
 - $\alpha = 1$: energy saving only
 - $0 < \alpha < 1$: trade-off between the two objectives





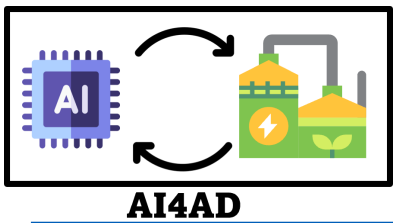
AI4AD

Artificial Intelligence Enabling Future Optimal Flexible Biogas Production for Net Zero

Funded by UKRI AI for Net-Zero

May 2023 – April 2025

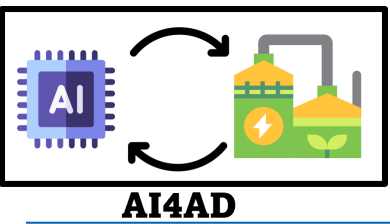




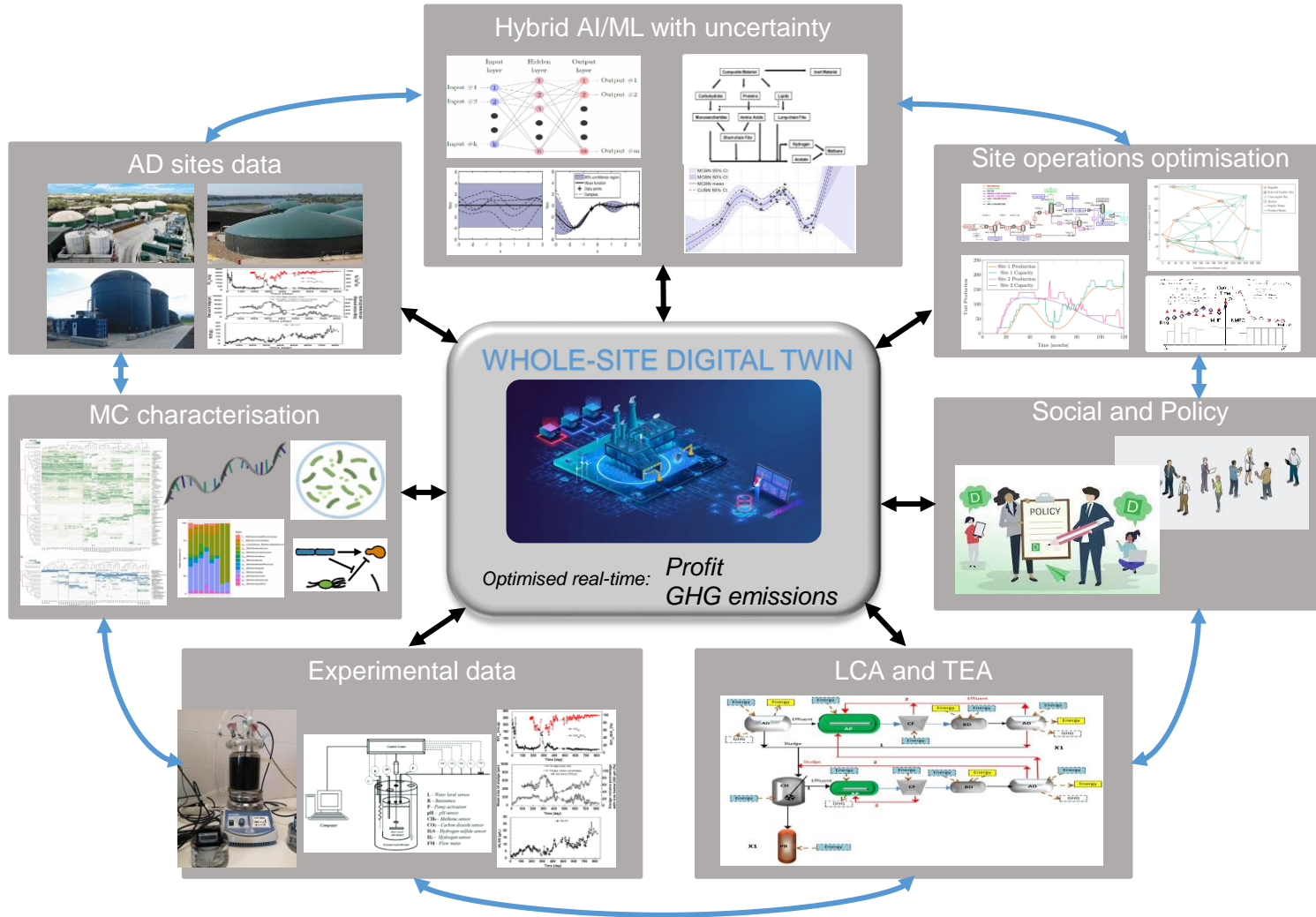
Project Overview

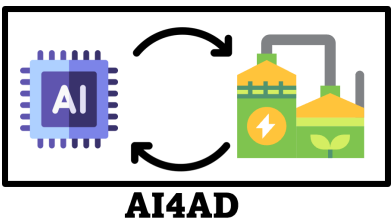
In this project, we will develop new tools to increase flexibility and profitability of anaerobic digestion for biogas production in the UK. We will link the various feedstocks (and their combinations) to the microbial populations and productivity of the biodigester, along with developing whole-systems AD site optimisation. We plan to do this by developing decision-making tools including:

- **Uncertainty-aware Hybrid Machine Learning Biodigester Digital Twin**
- **Optimisation-based system models of feedstock procurement and operation for real-time whole-site optimisation**

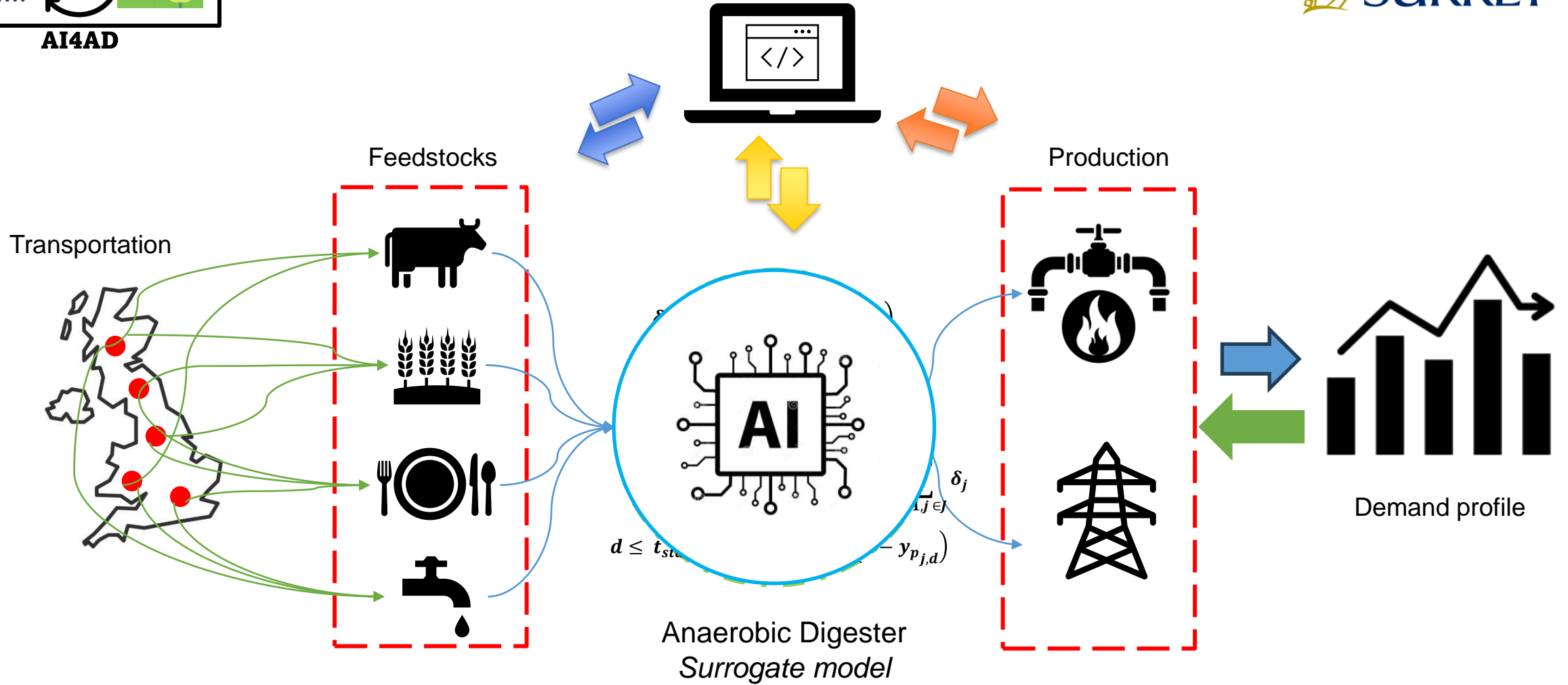


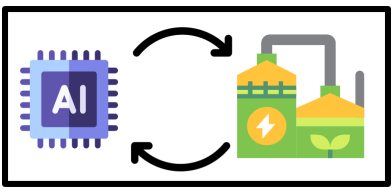
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Overview

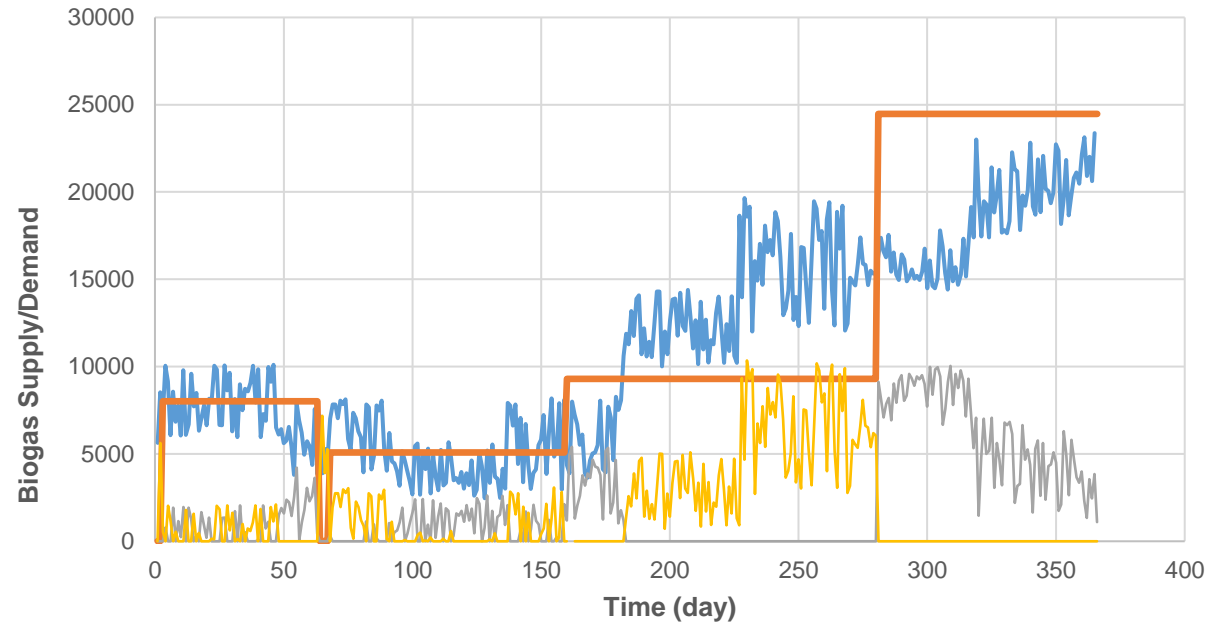




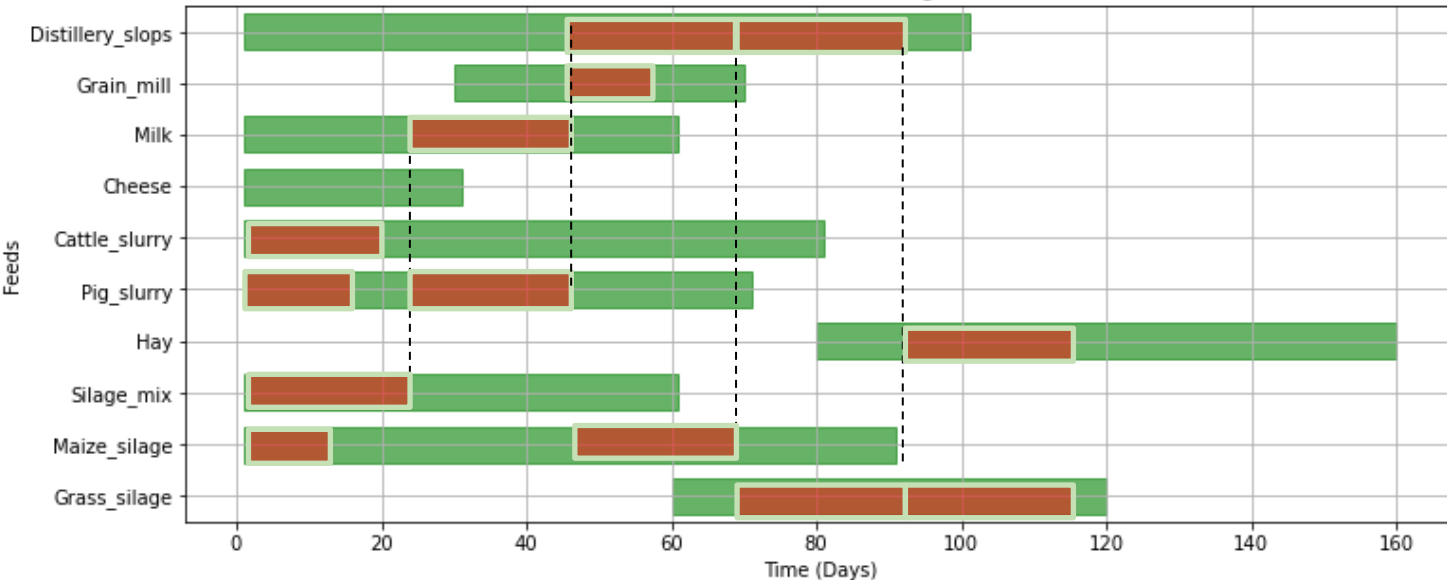
AI4AD

Demand-oriented feed scheduling

- A surrogate model is formulated to estimate the Co-Digestion effect.
- TBMP, EBMP, biomethane yield, C/N ratio, Total Solid (TS), Volatile Solid (VS), etc. considered.
- Considers storage losses.

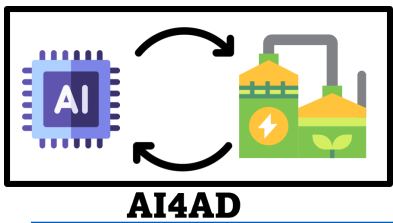


AD Plant Scheduling



— Demand — Production — Surplus — Deficit





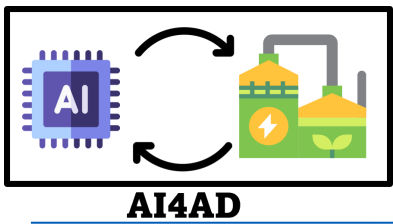
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Semi-continuous anaerobic digestion



- To study the effects of **feedstock, SRT, temperature and trace elements**
- To investigate **robustness and resilience of microbes** when encountering perturbations of operating conditions including the change in feedstock and extreme operational conditions
- To explore **new organic wastes as feedstock** to improve the acquisition of feedstock and reduce the reliance on energy crops
- To feed **lab-scale AD data/samples** to microbial study and process modelling teams and experimentally validate models in a quicker and easier manner

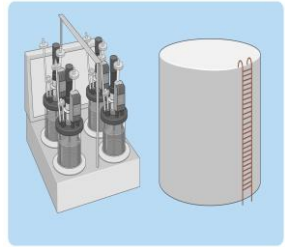
- **Biogas production**
 - Yield ($\text{m}^3/\text{ton VS feed}$)
 - Productivity ($\text{m}^3/(\text{m}^3 \cdot \text{d})$)
 - Biogas compositions (CH_4 , CO_2 , H_2 , H_2S , N_2O)
- **Digestate properties**
 - pH
 - Conductivity
 - ORP
 - FOS/TAC
 - TS and VS
 - VFAs and COD
 - Ammonia (TAN)
 - Nutrients and trace elements
 - Organic polymers (Cellulose, Proteins, Fats)



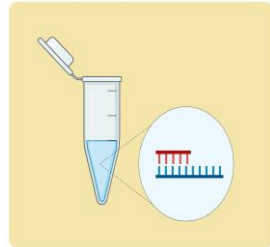
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Tools: Microbial ecology and systems microbiology

Simplified workflow



Lab reactor and full-scale samples

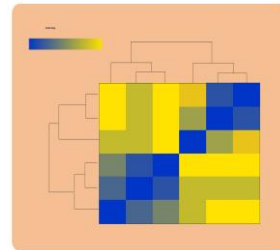


DNA and RNA extraction



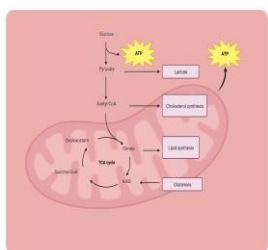
Molecular analysis

- Metagenomics
- Metatranscriptomics
- Metabolomics
- RT-qPCR



Data analysis (bioinformatics)

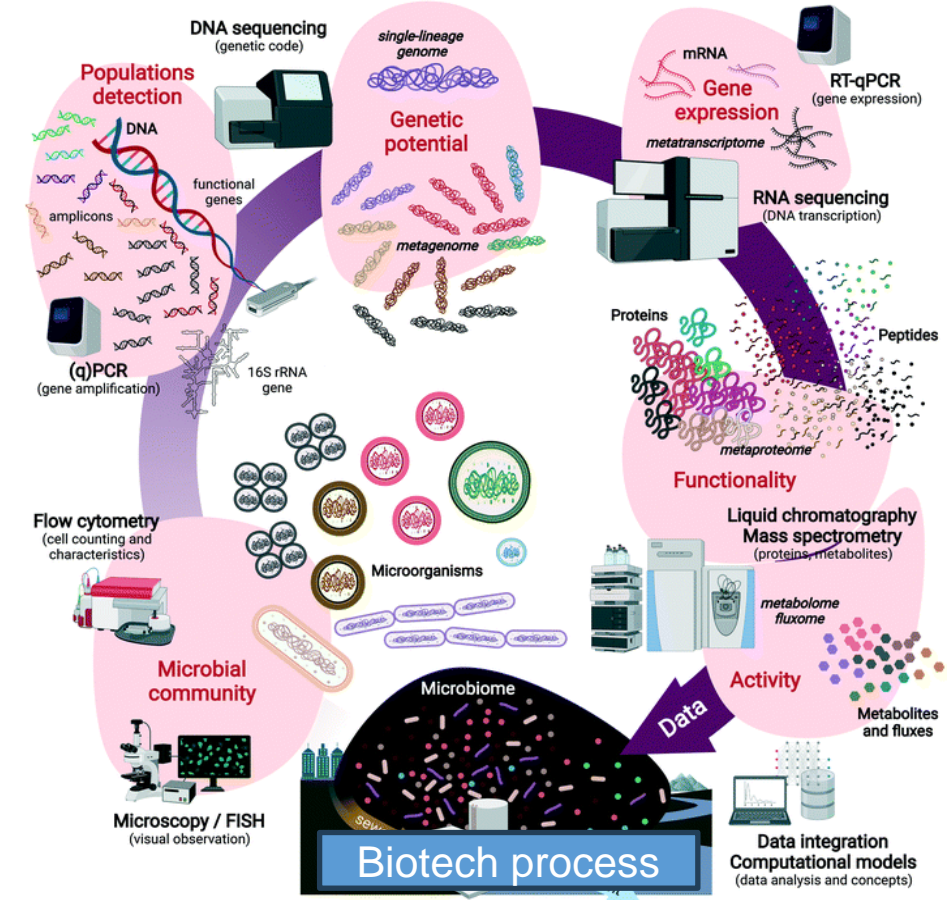
- Microbial community
- Gene expression
- Functionality

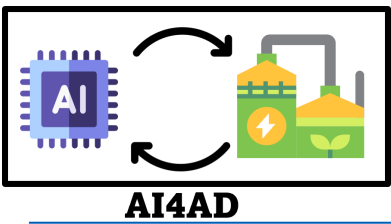


- Genome-scale metabolic network model
- Metabolites and fluxes

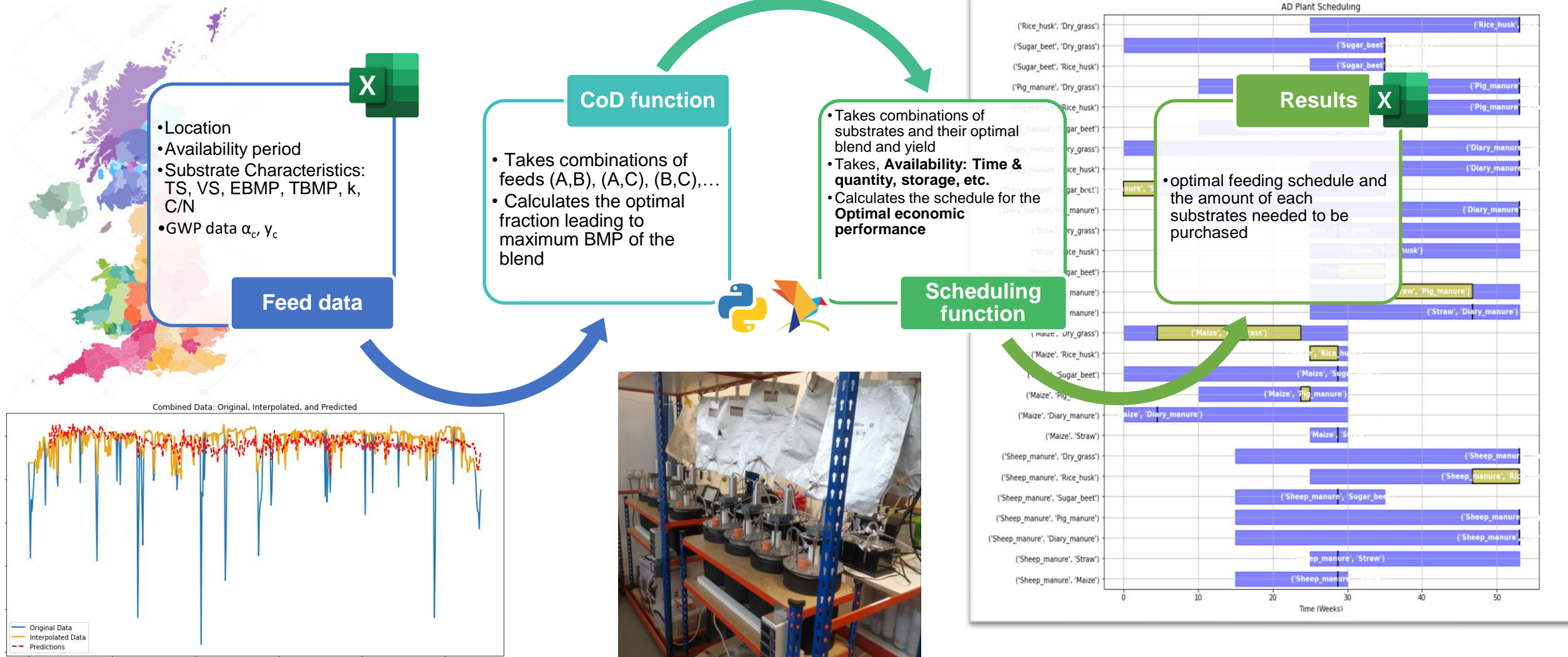
Design and control

Molecular microbiology analysis





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None of this would be possible without my wonderful team:
 Dr Ishanki De Mel, Rob Steven, Anamika Kushwah, Ruosi Zhang, Qingyuan Wang, Meshkat Dolat, Floris Bierkens, Gul Hameed, Dr Amin Zarei, Rohit Murali, Dr Benaissa Dekhici and others!



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